

## HEAT AND MASS TRANSFER IN MHD FREE CONVECTION FLOW OVER AN INCLINED STRETCHING PLATE WITH HALL CURRENT

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**Abstract-** The present paper is an investigation of heat and mass transfer of a steady flow of an incompressible electrically conducting fluid over an inclined stretching plate under the influence of an applied uniform magnetic field. The effects of Hall current are taken into account in this study where the flow is generated due to a linear stretching plate. Using suitable similarity transformations the governing equations of the problem are reduced to couple nonlinear ordinary differential equations and are solved numerically by Runge- Kutta fourth-fifth order method using symbolic software MATLAB. The numerical results concerned with the effects of various parameters of the flow fields on the velocity, secondary velocity temperature, and concentration profiles are investigated and presented graphically. The results have possible technological applications in liquid-based systems involving stretchable materials.

**Keywords:** MHD, Heat and mass transfer, Inclined Stretching plate, Chemical reaction, Hall current.

### 1. INTRODUCTION

The study of boundary layer flow and mass and heat transfer over an inclined stretching plate has generated much interest in recent years in view of its significant applications in industrial manufacturing processes such as glass-fiber, aerodynamic extrusion of plastic sheets, cooling of metallic sheets in a cooling bath, which would be in the form of an electrolyte and polymer sheet extruded continuously from a die are few practical applications of moving surfaces. Glass blowing, continuous casting, paper production, hot rolling, wire drawing, drawing of plastic films, metal and polymer extrusion, metal spinning and spinning of fibers also involve the flow due to stretching surface. During its manufacturing process a stretched sheet interacts with the ambient fluid thermally and mechanically. Both the kinematics of stretching and the simultaneous heating or cooling during such processes has a decisive influence on the quality of the final products [1]. In recent years, MHD flow problems have become more important industrially. Indeed, MHD laminar boundary layer behavior over a stretching surface is a significant type of flow having considerable practical applications in chemical engineering, electrochemistry and polymer processing. In the extrusion of a polymer sheet from a die,

the sheet is sometimes stretched. By drawing such a sheet in a viscous fluid, the rate of cooling can be controlled and the final product of the desired characteristics can be achieved. This problem has also an important bearing on metallurgy where magnetohydrodynamic (MHD) techniques have recently been used. Crane [2] first introduced the study of steady two-dimensional boundary layer flow caused by a stretching sheet whose velocity varies linearly with the distance from a fixed point in the sheet. Later on several researchers: Gupta and Gupta [3], Rajagopal et al. [4], Siddapa and Abel [5], Chen and Char [6], Laha et al. [7], Vajravelu and Nayfeh [8], Sonth et al. [9], and Tan et al. [10] studied various aspects of this problem, such as the heat, mass and momentum transfer in viscous flows with or without suction or blowing. The influence of a uniform transverse magnetic field on the motion of an electrically conducting fluid past a stretching sheet was investigated by Pavlov [11], Chakraborty and Gupta [12], Kumari et al. [13], Andersson [14], Andersson et al. [15], and Char [16]. The effect of chemical reaction on free-convective flow and mass transfer of a viscous, incompressible and electrically conducting fluid over a stretching sheet was investigated by Afify [17] in the presence of transverse magnetic field. Cortell [18] studied the magneto

hydrodynamics flow of a power-law fluid over a stretching sheet. Abel and Mahesh [19] presented an analytical and numerical solution for heat transfer in a steady laminar flow of an incompressible viscoelastic fluid over a stretching sheet with power-law surface temperature, including the effects of variable thermal conductivity and non-uniform heat source and radiation. Samad and Mohebujjaman [20] investigated the case along a vertical stretching sheet in presence of magnetic field and heat generation. Jhankal and Kumar [21] studied MHD boundary layer flow past a stretching plate with heat transfer. As many natural phenomena and engineering problems are worth being subjected to MHD analysis, the effect of transverse magnetic field on the laminar flow over a stretching surface was studied by a number of researchers [22-23]. Singh [16] studied heat and mass transfer in MHD boundary layer flow past an Inclined Plate with Viscous Dissipation in Porous Medium. Hall effects on MHD boundary layer flow over a continuous semi-infinite flat plate moving with a uniform velocity in its own plane in an incompressible viscous and electrically conducting fluid in the presence of a uniform transverse magnetic field were investigated by Watanabe and Pop [24]. Aboeldahab and Elbarbary [25] studied the Hall current effects on MHD free-convection flow past a semi-infinite vertical plate with mass transfer. The effect of Hall current on the steady magnetohydrodynamics flow of an electrically conducting, incompressible Burger's fluid between two parallel electrically insulating infinite planes was studied by Rana et al. [26]. Since the study of heat and mass transfer is important in some cases, in the present paper we studied the Hall effects on the steady MHD free-convective flow and mass transfer over an inclined stretching sheet in the presence of a uniform magnetic field. The boundary layer equations are transformed by a similarity transformation into a system of coupled non-linear ordinary differential equations and which are solved numerically by shooting iteration technique along with Runge- Kutta fourth-fifth order method. Numerical calculations were performed for various values of the magnetic parameter, Hall parameter and the relative effect of chemical diffusion on thermal diffusion parameters. The results are discussed from the physical point of view. Such a study is also applicable to the elongation to the bubbles and in bioengineering where the flexible surfaces of the biological conduits, cells and membranes in living systems are typically lined or surrounded with fluids which are electrically conducting (e.g., blood) and being stretched constantly.

## 2. MATHEMATICAL FORMULATION OF THE PROBLEM

Consider a two dimensional steady laminar MHD viscous incompressible electrically conducting fluid along an inclined stretching plate with an acute angle  $\gamma$ . X direction is taken along the leading edge of the inclined stretching plate and y is normal to it and extends parallel to x-axis. A magnetic field of strength  $B_0$  is introduced to the normal to the direction to the flow. The uniform plate temperature  $T_w (>T_\infty)$ , where  $T_\infty$  is the temperature of the fluid far away from the plate. Let  $u$ ,  $v$  and  $w$  be the

velocity components along the x and y axis and secondary velocity component along the z axis respectively in the boundary layer region. The sketch of the physical configuration and coordinate system are shown in Fig.1.

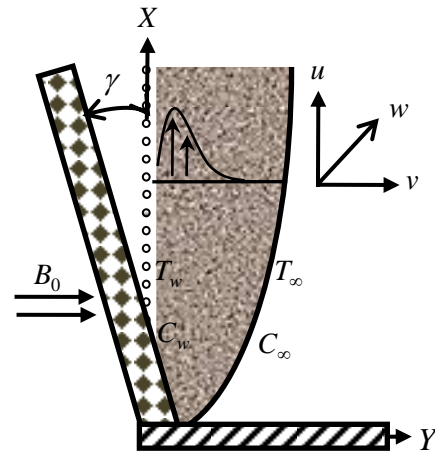


Fig.1 Physical configuration and coordinate system.

Under the above assumptions and usual boundary layer approximation, the dimensional governing equations of continuity, momentum, concentration and energy under the influence of externally imposed magnetic field are:

$$\text{Equation of continuity: } \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (1)$$

Momentum equation:

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \nu \frac{\partial^2 u}{\partial y^2} + g\beta(T - T_\infty)\cos\gamma + g\beta^*(C - C_\infty)\cos\gamma - \frac{\sigma B_0^2 \mu_e}{\rho(1+m^2)}(u + mw) \quad (2)$$

$$u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} = \nu \frac{\partial^2 w}{\partial y^2} + \frac{\sigma B_0^2 \mu_e}{\rho(1+m^2)}(mu - w) \quad (3)$$

Energy Equation:

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \frac{\partial^2 T}{\partial y^2} + \frac{\nu}{c_p} \left[ \left( \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial w}{\partial y} \right)^2 \right] \quad (4)$$

Concentration Equation:

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D \frac{\partial^2 C}{\partial y^2} - K_0(C - C_\infty)^n \quad (5)$$

Boundary conditions are:

$$u = bx, v = w = 0, T = T_w, C = C_w \quad \text{at } y = 0$$

$$u = 0, w = 0, T = T_\infty, C = C_\infty \quad \text{as } y \rightarrow \infty$$

To convert the governing equations into a set of similarity equations, we introduce the following

transformation:

$$u = bx f'(\eta), v = -\sqrt{b\nu} f(\eta), w = bx g_0(\eta), \eta = y \sqrt{\frac{b}{\nu}}$$

$$\theta(\eta) = \frac{T - T_\infty}{T_w - T_\infty}, \varphi(\eta) = \frac{C - C_\infty}{C_w - C_\infty}$$

From the above transformations, the non-dimensional, nonlinear and coupled ordinary differential equations are obtained as

$$f''' + ff'' - f'^2 + G_r \theta \cos \gamma + G_c \varphi \cos \gamma - \frac{M}{1+m^2} (f' + mg_0) = 0 \quad (6)$$

$$g_0'' + fg_0' - \left( f' + \frac{M}{1+m^2} \right) g_0 + \frac{Mm}{1+m^2} f' = 0 \quad (7)$$

$$\theta'' + Pr f \theta' + Pr Ec (f'^2 + g_0'^2) = 0 \quad (8)$$

$$\varphi'' + Sc f \varphi' - Sc \zeta \varphi^n = 0 \quad (9)$$

Where the notation primes denote differentiation with respect to  $\eta$  and the parameters are defined as

$$G_r = \frac{g\beta(T_w - T_\infty)}{b^2 x}, Pr = \frac{\mu}{\alpha}, M = \frac{\sigma B_0^2}{\rho b},$$

$$Ec = \frac{c_p b^2 x^2}{\nu^2 (T_w - T_\infty)}, \zeta = \frac{K_0 (C_w - C_\infty)^{n-1}}{b},$$

$$Sc = \frac{g\beta^* (C_w - C_\infty)}{b^2 x}, S_c = \frac{\nu}{D_m}, \alpha = \frac{K}{\rho c_p}$$

The transform boundary conditions:

$$f = 0, f' = 1, g = 0, \theta = \varphi = 1 \quad \text{at } \eta = 0$$

$$f = f' = g = \theta = \varphi = 0 \quad \text{as } \eta \rightarrow \infty$$

### 3. RESULTS AND DISCUSSION

The system of ordinary differential equations (6)-(9) subject to the boundary conditions is solved numerically by shooting iteration technique along with Runge-Kutta fourth-fifth order method using symbolic software. We have formulated the effect of Hall Parameter ( $m$ ), Magnetic parameter ( $M$ ), Prandtl number ( $Pr$ ), Eckert number ( $Ec$ ), Schmidt number ( $Sc$ ), Grashof number ( $G_r$ ) and reaction parameter ( $\zeta$ ) of an incompressible fluid over an inclined stretching plate. The numerical calculation for the distribution of primary velocity, secondary velocity, temperature and concentration across the boundary layer for different values of the parameters are carried out. For the purpose of our computation, we

have chosen the various values of parameters. Fig.2- Fig.9 depicts the variation of velocity profiles for different values of various parameters. From the Fig.2 it is seen that the velocity starts from minimum value at the surface and increase till it attain peak value and then starts decreasing until it reaches to the minimum value at the end of the boundary layer for all the values of magnetic field parameter. It is interesting to note that the effect of magnetic field is more prominent at the point of peak value, because the presence of  $M$  in an electrically conducting fluid introduces a force called Lorentz force which acts against the flow if the magnetic field is applied in the normal direction, as in the present problem. Thus we conclude that  $M$  be used to control the flow characteristic. From Fig.7 it is observed that the secondary velocity increase with an increase in the  $M$ . From Fig.5 it is seen that as  $G_r$  increases the velocity field decreases. This cause the velocity buoyancy effects to decreases yielding a reduction in the fluid velocity. The reductions and the velocity profiles are accompanied by simultaneous reductions in the velocity boundary layers. From Fig. 6 the velocity decreases as the increase in  $Ec$ . From Fig. 3 the velocity increases as the increase in  $m$  but from Fig. 8 it is observed that an increasing in Hall parameter leads to decrease in secondary velocity profiles. This is due to the facts that the effective conductivity increases with the increase in Hall parameter which raises the magnetic damping force hence decreasing the velocity. From Fig.4 it is observed that in the neighborhood of the plate the primary velocity decrease and far away from the plate the velocity increase for the inclination of the plate but Fig.9 indicates that the secondary velocity increases as increase of inclination of the plate. Fig.10 shows that temperature increase for increasing values of  $M$  because of decreasing heat flux. As results boundary layer thickness increases. Similar trend is observed in Fig.11 for increasing values of  $m$  because of excess heating consequently decreases heat flux. As a result boundary layer thickness increases in the case of fluid withdrawing as well as for fluid injecting. Therefore  $m$  and  $M$  can be used to control heat transfer characteristic. From Fig.12 and Fig. 14 it is seen that temperature decrease for increasing values of  $Ec$  and  $\gamma$ . Fig.13 illustrates the temperature profiles for various values of  $Pr$ . It is observed that the temperature decrease as an increasing the  $Pr$ . the reason is that smaller values of  $Pr$  are equivalent to increase in the thermal conductivity of the fluid and therefore heat is able to diffuse away from the heated surface more rapidly for higher values of  $Pr$ . Hence in the case of smaller  $Pr$  the thermal boundary layer is thicker and the rate of heat transfer is reduced. Fig.15 – Fig.18 display the effect of  $M$ ,  $m$ ,  $\gamma$  and  $\zeta$  respectively. For various values of  $M$ ,  $m$ ,  $\gamma$  and  $\zeta$  concentration profile decrease but the variation of concentration is negligible for  $M$  and  $m$ . In Fig.19 it is observed that concentration profile decrease for increasing values of mass diffusion parameter  $Sc$  because increasing in  $Sc$  decreases molecular diffusivity which results a decrease of the concentration boundary layer. Hence the concentration of the species is lower for large values of  $Sc$ .

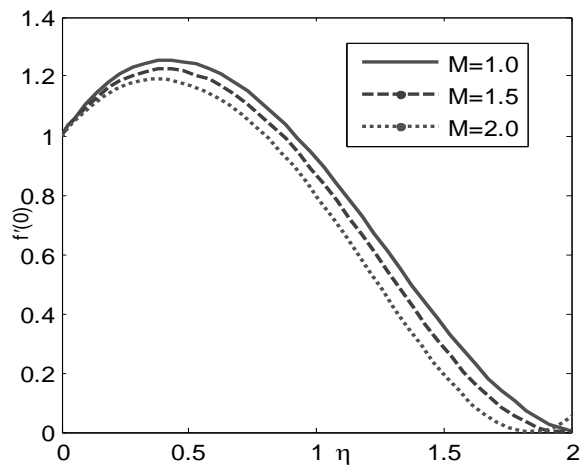


Fig. 2. Velocity profile for various values of  $M$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

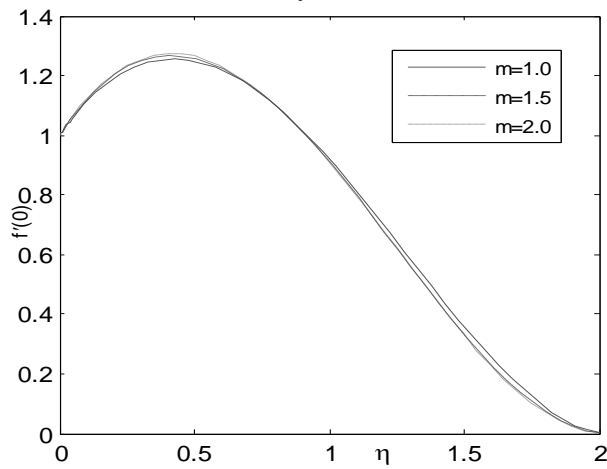


Fig. 3. Velocity profile for various values of  $m$  and  $M=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

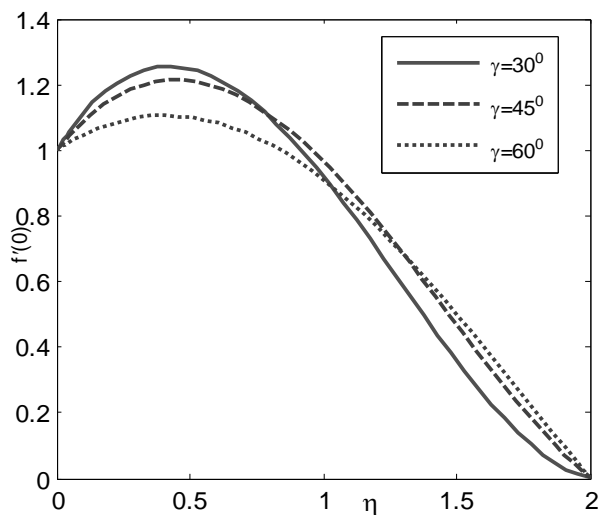


Fig. 4. Velocity profile for various values of  $\gamma$  and  $m=1.0$ ,  $M=1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

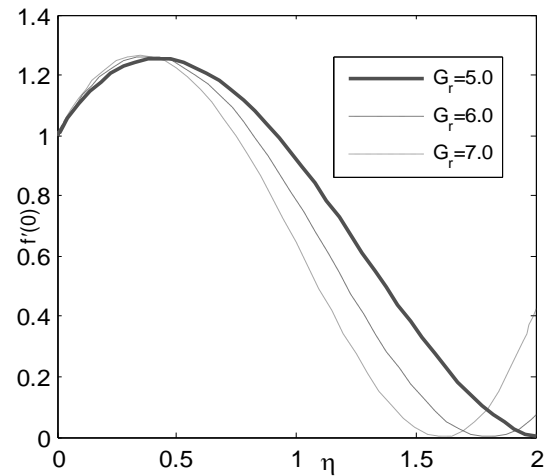


Fig. 5. Velocity profile for various values of  $G_r$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $M=1.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

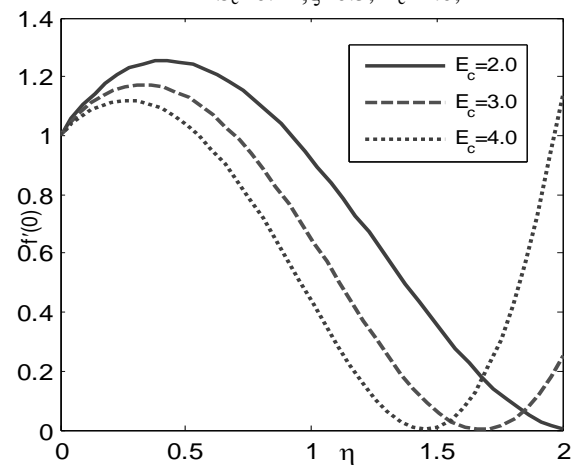


Fig. 6. Velocity profile for various values of  $E_c$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $M=1.0$ ,  $n=2$

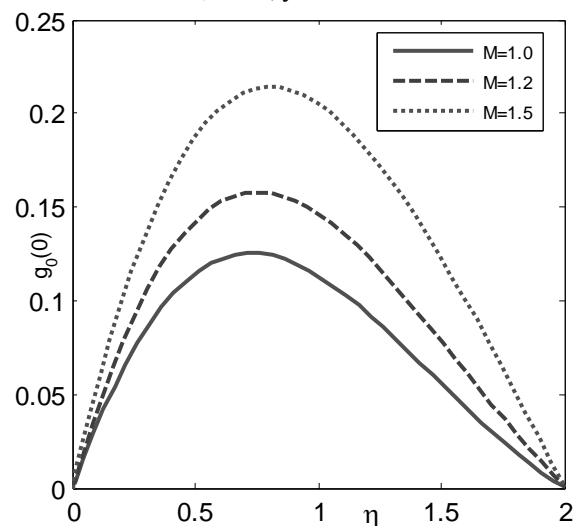


Fig. 7. Secondary Velocity profile for various values of  $M$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

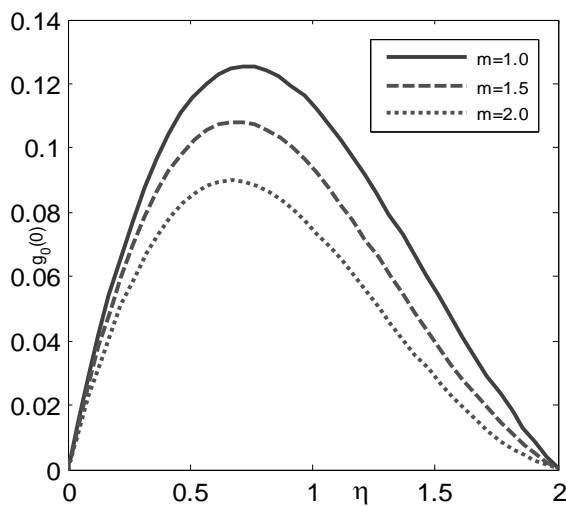


Fig. 8. Secondary Velocity profile for various values of  $m$  and  $M=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

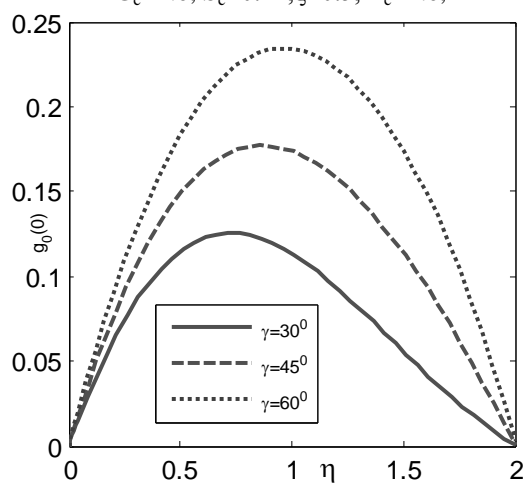


Fig. 9. Secondary Velocity profile for various values of  $\gamma$  and  $m=1.0$ ,  $M=1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

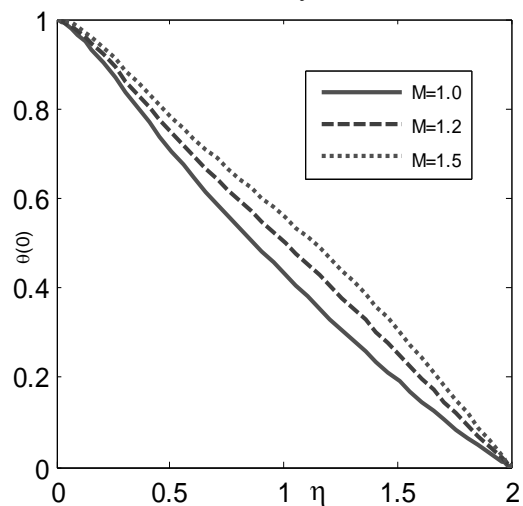


Fig. 10. Temperature profile for various values of  $M$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

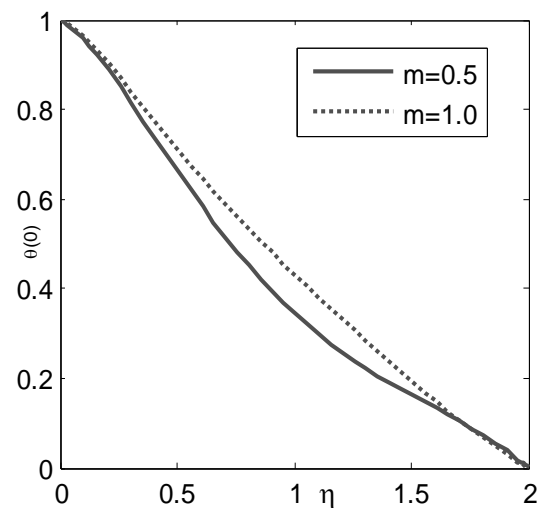


Fig. 11. Temperature profile for various values of  $m$  and  $M=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

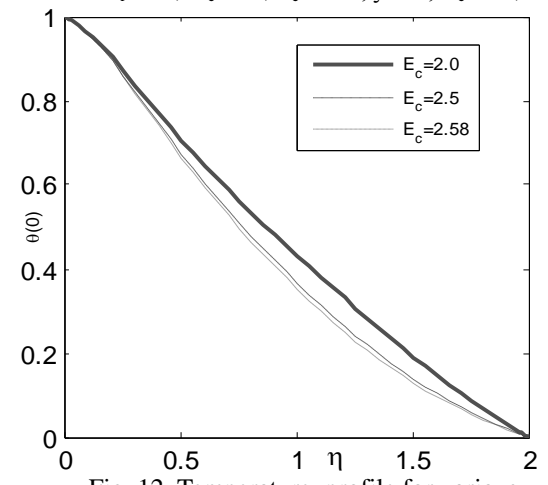


Fig. 12. Temperature profile for various values of  $E_c$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $M=1.0$ ,  $n=2$

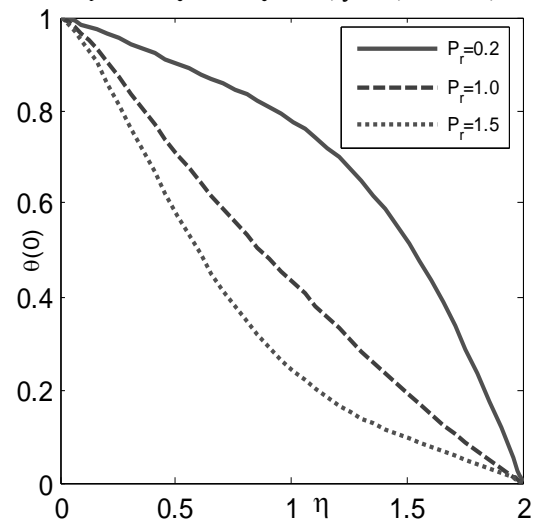


Fig. 13. Temperature profile for various values of  $P_r$  and  $m=1.0$ ,  $\gamma=30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $M=1.0$ ,  $n=2$ ,  $E_c=2.0$

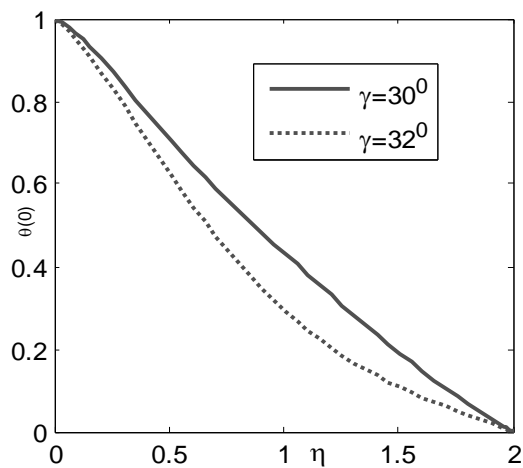


Fig. 14. Temperature profile for various values of  $\gamma$  and  $m=1.0$ ,  $M = 1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

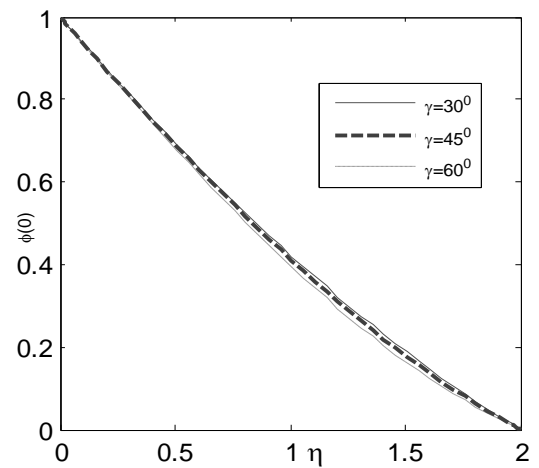


Fig. 17. Concentration profile for various values of  $\gamma$  and  $m=1.0$ ,  $M = 1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

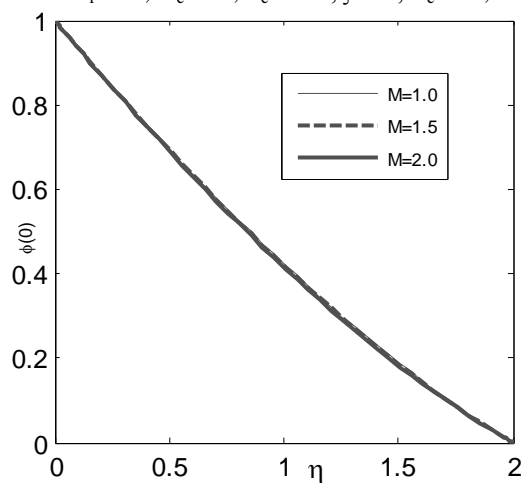


Fig. 15. Concentration profile for various values of  $M$  and  $m=1.0$ ,  $\gamma = 30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

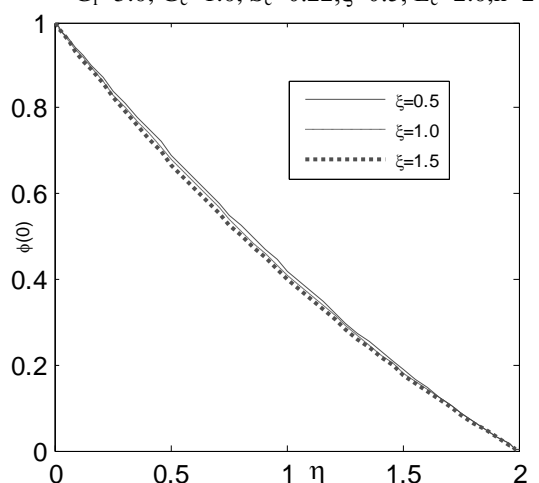


Fig. 18. Concentration profile for various values of  $\xi$  and  $m=1.0$ ,  $M = 1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $E_c=2.0$ ,  $n=2$ ,  $\gamma = 30^\circ$

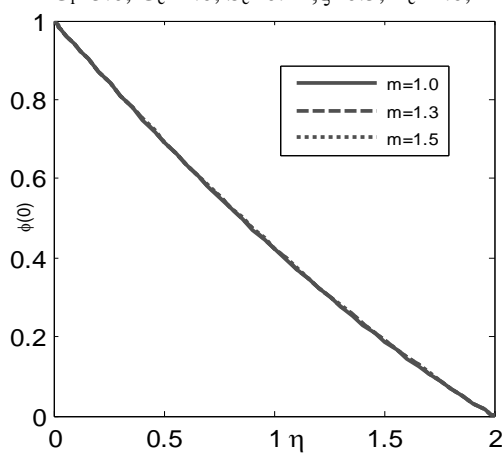


Fig. 16. Concentration profile for various values of  $m$  and  $M=1.0$ ,  $\gamma = 30^\circ$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $S_c=0.22$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$

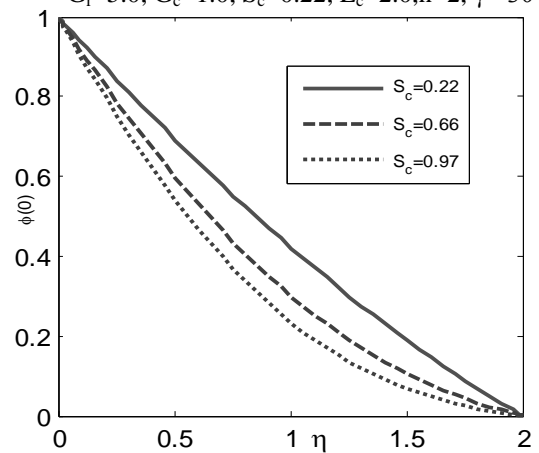


Fig. 19. Concentration profile for various values of  $S_c$  and  $m=1.0$ ,  $M = 1.0$ ,  $P_r=1.0$ ,  $G_r=5.0$ ,  $G_c=1.0$ ,  $\xi=0.5$ ,  $E_c=2.0$ ,  $n=2$ ,  $\gamma = 30^\circ$

#### 4. CONCLUSION

In this Paper the effects of Hall current parameter on free-convective flow heat and mass transfer of a viscous, incompressible and electrically conducting fluid over an inclined stretching plate have been studied in the presence of magnetic field. Numerical solutions are obtained through shooting method. The observations are that the velocity profile decreases with the increase in the magnetic parameter  $M$ , which is significant, but the velocity increases with the increase in the Hall parameter  $m$  and the velocity decreases with the increase in the inclination  $\gamma$  near the plate and increases far away from the plate. The secondary velocity fields increases with the increase of magnetic parameter  $M$ , but secondary velocity decreases with the increase of Hall parameter  $m$ . The temperature increases for increasing values of  $M$  and  $m$ , but decreases for the values of  $\gamma$ ,  $E_c$  and  $P_r$ . The concentration decreases for the increase of  $M$ ,  $m$ ,  $\xi$ ,  $S_c$  and  $\gamma$ .

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## 7. NOMENCLATURE

| Symbol            | Meaning   |
|-------------------|---|
| MHD               | Magnetohydrodynamics                                  |
| $c_p$             | Specific heat of with constant pressure               |
| $g$               | Gravitational acceleration                            |
| $g_0$             | Secondary Velocity                                    |
| $f'$              | Velocity Profile                                      |
| $M$               | Magnetic parameter                                    |
| $m$               | Hall parameter  |
| $\nu$             | Kinematic viscosity                                   |
| $\gamma$          | Inclination of the Plate                              |
| $\eta$            | Similarity variable                                   |
| $\alpha$          | Thermal diffusivity                                   |
| $\beta$           | Thermal Expansion Coefficient                         |
| $\beta^*$         | Coefficient of expansion with concentration           |
| $\rho$            | Density   |
| $\sigma$          | Fluid electrical conductivity                         |
| $\theta$          | Dimensionless temperature                             |
| $u$               | Velocity component in x-direction                     |
| $v$               | Velocity component in y-direction                     |
| $w$               | Secondary Velocity                                    |
| $T$               | Temperature   |
| $K_0$             | Reaction rate constant                                |
| $D_m$             | Thermal molecular diffusivity                         |
| $C$               | Concentration   |
| $C_\infty$        | Concentration of the fluid outside the boundary layer |
| $n$               | Order of reaction                                     |
| $P_r$             | Prandle number  |
| $G_r$             | Grashof number  |
| $G_c$             | Modified Grashof number                               |
| $E_c$             | Eckert number   |
| $S_c$             | Schmidt number  |
| $\xi$             | Non-dimensional chemical reaction parameter           |
| $B_0$             | Constant magnetic field intensity                     |
| $T_w$             | Temperature at the Plate                              |
| $T_\infty$        | Temperature of the fluid outside the boundary layer   |
| <b>Subscripts</b> |   |
| w                 | Quantities at wall                                    |
| $\infty$          | Quantities at the free stream                         |